

Study on Tool Condition Parameters Intended for Smart Tool Management in Filleted End Milling

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ABSTRACT

Filleted end milling is commonly used as a versatile manufacturing process, whereas the optimization for tool condition management is one of the continuously noticed topics. It can also contribute to the achievement of Sustainable Development Goals. A lot of outcomes have been reported so far in the experimental investigations of tool condition parameters. However, the findings and knowledge from theoretical perspective are relatively scarce to advance smart tool management. Hence, the aim of this study is to give theoretical consideration with tool condition parameters. The investigations focus on filleted end milling with some variations of machining conditions. Several tool condition parameters were theoretically proposed after illustrating geometrical modeling with variable description. Then, the demonstrations and discussion were made based on the computational results in filleted end milling. The results visually and numerically ascertained novel findings regarding several characteristics of tool condition parameters.

Keywords: tool condition parameter, machining condition, optimization, multi-axis CNC machining, filleted end mill.

INTRODUCTION

These days, Sustainable Development Goals have gradually come to pervade various aspects of our society. Sustainable manufacturing has resultantly been attracting global-scale attention from industries, academics, governments, etc. over the last decades [1, 2]. Under the backgrounds, the contributions with high potential were made from a variety of perspectives [3–6]. In mechanical machining, sustainability appearing in each stage of the process is recognizable as one of the important, challenging opportunities toward the achievement of Sustainable Development Goals [7]. Moreover, it is well known that poor cutting tool management leads to a tremendous loss of productivity and profits. There are various viewpoints of studies focusing on efficient tool management not only to enlarge tool life but also to prevent tool wear and failure [8–10]. Tool condition monitoring has been conducted as one of the potential methods in some of

these studies [11–14]. The smart approach is also being proposed with information and communication technologies [15, 16]. The sophistication of these methods is desired more and more for enhancing machining efficiency, reducing the frequency of tool replacement and so on. Although experimental investigation of the controlling factors has been made in direct and indirect manners, the theoretical one is still immature to implement it into smart manufacturing system. In addition, it is computationally riskful that the extant factors include ambiguity. Thus, the further essential factors must have great potential to establish the smart tool management exploiting one of the sustainable breakthroughs in manufacturing process. They can also inspire the development of suitable hybrid approaches with theory and practice.

Milling is one of the core technologies with a versatile, highly-automated process in today's industry. Computer numerical controlled (CNC) machine tools have broadly used to advance manufacturing automation [17–19]. CNC machining

technology gradually pervaded its applicable fields with the development of CNC machine tools. Computer-aided technologies have also added impetus to the technological advancement. Computer-aided design became one of the driving forces to create attractive products [20]. A designed shape made in computer-aided design has indispensable influence on product manufacturing. Computer-aided manufacturing is also a crucial technology for the modern production [21, 22]. A process plan with machining parameters' selection in computer-aided manufacturing is vital for surface quality, machining accuracy, etc. in practical manufacturing [23–30]. These technologies are playing an essential role in smart manufacturing, whereas the accumulated findings and knowledge are still insufficient for the practical use in smart technologies.

There are various methodologies aimed at an optimization of machining parameters in milling. Cutting force is a high-interest topic not only to avoid tool failure but also to enhance finish surface quality. Lazoglu et al. reported a feedrate scheduling technique based on their force model [31]. Habibi et al. also proposed a computationally-inexpensive approach minimizing flute engagement to adjust tool orientation for optimizing surface errors in five axis ball end milling [32]. Moreover, cutter/workpiece engagement is one of the important factors to figure out suitable processing parameters. Zhang et al. studied an optimization of tool orientation in 5-axis ball-end milling through a model of cutter/workpiece engagement [33]. Chip thickness is theoretically modeled to determine the other machining factors. Lotfi et al. provided a model of instantaneous undeformed chip thickness [34]. Residual stress in machined surface is also a measure to optimize processing parameters; in addition, Masmiaati and Sarhan revealed an influence of cutting parameters on residual stress in machined surfaces [35]. The other related works were also published in many kinds of medium [36–39]. Although there are dominant processing parameters' optimizations from various perspectives, a few comprehensive strategies have been proposed to determine machining conditions in filleted end milling. Accordingly, the accumulation of findings and knowledge is imperative for intelligent use of information toward the development of smart technologies.

In this study, theoretical investigations with tool condition parameters were given for the further advancement of smart manufacturing. They

focus particularly on filleted end milling with some variations of tool rotational speed, feed rate, and tool orientation. Several tool condition parameters will be theoretically proposed after illustrating geometrical modeling with variable description. Then, the demonstrations and discussion will be made based on the computational results in filleted end milling. The results visually and numerically will reveal novel findings regarding several characteristics of tool condition parameters.

Modeling with variable description

Several coordinate systems is firstly provided to express a machining state of filleted end milling. Henceforth, an axis of a coordinate system is invariably denoted by a normalized vector. This study introduces three coordinate systems as shown in Figure 1.

These right-handed coordinate systems are labelled as G, M, and T. G coordinate system comprises X , Y , Z axes, whose components are $(1, 0, 0)$, $(0, 1, 0)$, and $(0, 0, 1)$, respectively. M coordinate system is also defined based on a surface to be machined. MZ is a unit surface normal on a workpiece. MY is orthogonal to MX , and it is oriented to the scanning direction of a tool; moreover, MY can be obtained from the cross product of MX and MZ .

Two sections are instantaneously set to consider the other coordinate system and inclination angles in filleted end milling. The one is a section based on the scanning direction of a tool (i.e., $MZ - MX$ plane), while the other is a section based on the cross-feed direction perpendicular to the scanning direction (i.e., MZ

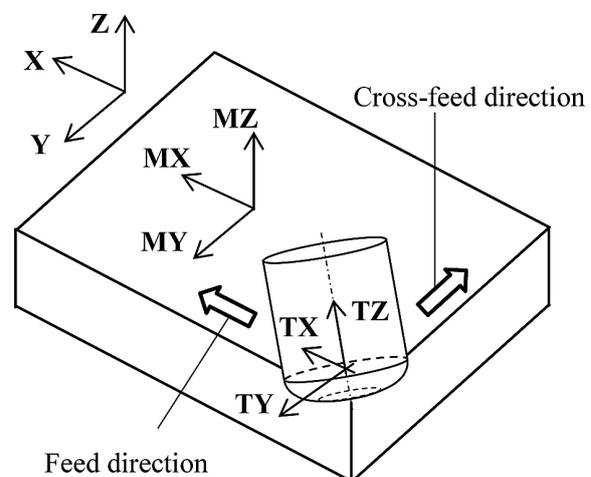


Fig. 1. Three coordinate systems in filleted end milling

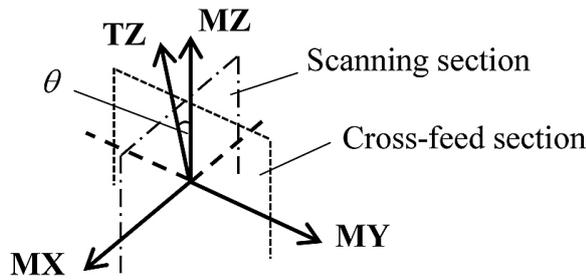


Fig. 2. Two instantaneous sections and tool inclination angle θ between MZ and TZ

- MY plane). Let these planes be scanning section and cross-feed section, respectively. T coordinate system can be expressed using the two sections. The position of TZ corresponds to that of the rotational axis of a tool, and the direction is oriented to the shank side of tool. As illustrated in Figure 2, tool inclination angle θ denotes the angle between MZ and TZ . TX is geometrically calculated as a vector perpendicular to TZ . The direction depends on the directional relationship between TZ and MZ . Specifically, the angle between TX and $MX - MY$ plane is inevitably set to be θ . Then, TY can be obtained from the cross product of TX and TZ .

The angles θ_s and θ_c are additionally introduced to derive θ . As shown in Figure 3, θ_s is the inclination angle on scanning section, designating the angle between MZ and the orthogonal projection of TZ onto scanning section. Likewise, θ_c is the inclination angle on cross-feed section, indicating the angle between MZ and the orthogonal projection of TZ onto cross-feed section. Counterclockwise rotation is the positive rotational direction of θ_s and θ_c .

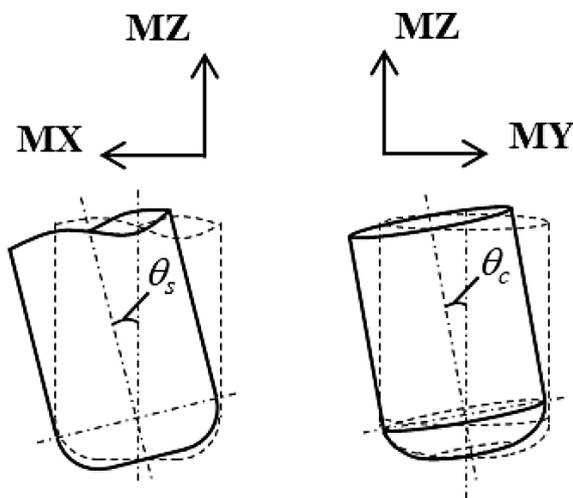


Fig. 3. Inclination angles θ_s and θ_c

Given that M coordinate system coincides completely with G coordinate system for simple modeling of filleted end milling, θ_s and θ_c can be calculated as follows:

$$\theta_s = \cos^{-1} \left(\frac{TZ_z}{\sqrt{TZ_y^2 + TZ_z^2}} \right) \quad (1)$$

$$\theta_c = \cos^{-1} \left(\frac{TZ_z}{\sqrt{TZ_x^2 + TZ_z^2}} \right) \quad (2)$$

where: TZ_x , TZ_y , and TZ_z are three components of TZ in each axis of G coordinate system. Since TZ is given as a normalized vector,

$$TZ_x^2 + TZ_y^2 + TZ_z^2 = 1 \quad (3)$$

Hence, Equations (1) and (2) can lead to the following components of TZ :

$$TZ_x = TZ_z \tan \theta_s \quad (4)$$

$$TZ_y = -TZ_z \tan \theta_c \quad (5)$$

Substituting Equations (4) and (5) to Equation (3) provides the following formula:

$$TZ_z = \sqrt{\frac{1}{\tan^2 \theta_c + \tan^2 \theta_s + 1}} \quad (6)$$

Accordingly, the angle θ can be offered as an inverse trigonometric function with TZ_z :

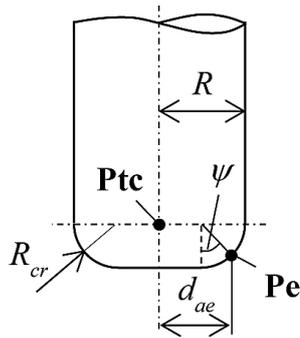
$$\theta = \cos^{-1} \left(\frac{TZ_z}{\sqrt{TZ_x^2 + TZ_y^2 + TZ_z^2}} \right) = \cos^{-1}(TZ_z) \quad (7)$$

Figure 4 illustrates the positional relationship of two cutting edges in filleted end mill. Although there exist various kinds of cutting edge geometry, this study focuses on a filleted end mill with two flutes and without a helix angle of cutting edges. It means that the filleted end milling is not oblique process. With reference to Figure 4, a cutting point on a cutting edge in T coordinate system TPe can be calculated as follows: when $d_{ae} \geq R - R_{cr}$,

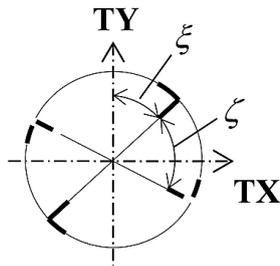
$$TPe_x = ((R - R_{cr}) + R_{cr} \sin \psi) \sin(\xi + \zeta)$$

$$TPe_y = ((R - R_{cr}) + R_{cr} \sin \psi) \cos(\xi + \zeta) \quad (8)$$

$$TPe_z = -R_{cr} \cos \psi$$



(a) Typical tool profile



(b) Cutting edges' position in TX - TY plane

Fig. 4. Typical tool profile and cutting edges' position

and when $d_{ae} < R - R_{cr}$,

$$\begin{aligned} TPe_x &= d_{ae} \sin(\xi + \zeta) \\ TPe_y &= d_{ae} \cos(\xi + \zeta) \\ TPe_z &= -R_{cr} \end{aligned} \quad (9)$$

It should be careful that clockwise rotation is the positive rotational direction of ξ and ζ . Common end mills have a number of cutting edges, so that ξ depends on the number of cutting edges n_{ce} . In the case that the angular position of a cutting edge overlaps TX axis, ξ can be derived as a simple form:

$$\xi = (m - 1) \frac{2\pi}{n_{ce}} \quad (1 \leq m \leq n_{ce}) \quad (10)$$

where: m is an assigned number of a cutting edge.

From the above explanation, a cutting point on a cutting edge \mathbf{Pe} can be calculated through the following formula:

$$\mathbf{Pe} = \mathbf{R}_T \mathbf{TPe} + \mathbf{Ptc} \quad (11)$$

where: \mathbf{R}_T is coordinate transformation matrix, providing a transformation from T to O coordinate system; moreover, \mathbf{Ptc}

is an instantaneous tool center shown in Figure 4 (a), depending on a tool path up until a present position.

The geometrical description explained in this section assumes a filleted end mill without a helix angle of cutting edges, while it can effortlessly apply to the common, commercial ones through dividing a tool into small disk elements.

Tool condition parameters

This section theoretically provides tool condition parameters favorable for smart tool management. Especially, we focus on the parameters contributable for predicting tool life and wear. They are closely related to machining conditions. Thus, the decision-making step determining them is indispensable to achieve suitable machining conditions. The some theoretical procedures will be given below with the aim of optimal parameters' selection in filleted end milling. Note that the following calculations are unalterably given for one cutting edge during one rotation of a tool.

Maximum frictional distance

Frictional distance is a critical factor to predict tool wear at the cutting edge. It also has an influence on a machined surface feature. The following formula can provide the maximum length:

$$sl_{fd} = (R_{cr} \sin \alpha_{fd} + R_b) \beta_{fd} \quad (12)$$

In the above formula, α_{fd} is obtained from an arccosine calculation for a scalar product of \mathbf{u}_{sep} and $-\mathbf{TZ}$. Here, a directional vector \mathbf{u}_{sep} can be calculated as follows: a bull nose shape of filleted end mill is modeled as a torus created by a rotation of true circle about TZ axis. The circle's radius is identical to a corner radius of cutting edge, and a torus's section can be always set by rotating the true circle. In the filleted end milling, a single contact point between a workpiece's surface and the true circle inevitably arises at one moment during the rotation of cutting edge. Here, we consider the true circle's center at one moment when the single contact point arises. Then, a vector product can be calculated from a tangent vector to torus's major circle and a workpiece's surface normal. After that, \mathbf{u}_{sep} is obtained as a vector product of the tangent vector to torus's major circle and the vector calculated previously. These procedures can be effortlessly implemented using the computational

algorithm proposed in our previous study [29]. Moreover, a rotational angle around **TZ** axis β_{fd} is utilized as the one between **TX** - **TZ** plane and a center of torus section having a contact point with a workpiece's surface. The angles α_{fd} and β_{fd} can be given in the calculation process of computational algorithm.

Maximum contact arc length

Contact arc length is defined based on a cutting-related part in a cutting edge, so that it is also an important factor in considering tool surface damage and a machined surface feature. The maximum length can be expressed:

$$sl_{cal} = R_{cr}(\alpha_{cal} + \alpha_{hf}) \quad (13)$$

where: α_{cal} is easily identified from an angle calculation using R_{cr} and the depth of cut ap which means a distance between a designed surface and workpiece's surface principally.

In contrast, α_{hf} can be computed from an angle calculation based on a feed mark's height h_f . Here, h_f can be mathematically expressed in the same manner to path interval determination in ball end milling. The angle α_{hf} is also obtainable in the calculation process of computational algorithm.

Maximum cutting speed

It is well known that cutting speed has actual impact on both tool surface damage and cutting force. The following expression can be made to estimate the maximum cutting speed:

$$v_{cs} = 2\pi \left(R_b + R_{cr} \cos \left(\frac{\pi}{2} - (\theta + \alpha_{cs}) \right) \right) \frac{s}{1000} \quad (14)$$

where: s is a spindle speed in cutting process, and α_{cs} is easily identified using the depth of cut ap .

In the calculation process of computational algorithm, the angle α_{cs} is available under any conditions.

Average uncut chip thickness

Uncut chip thickness is one of the vital factors having great impact on cutting force. It is undoubted that uncut chip thickness affects tool surface damage in practice since cutting force directly depends on material removal rate in machining process. The following formula enables us to calculate the average value:

$$t_{uct} = f_t \sin \beta_{uct} \sin \alpha_{uct} \quad (15)$$

where: α_{uct} indicates an angular parameter for determining an arbitrary position on a cutting edge. In addition, β_{uct} designates an angle between **TX** axis and **GY** - **GZ** plane, and the rotation is about **TZ** axis.

The above formula can estimate an uncut chip thickness at any position on a cutting edge. As a brief estimation, an average uncut chip thickness t_{ave} was computed in a cutting edge's rotational position where the instantaneous cutting load and area were the largest in both measures, and three angles of α_{uct} were considered for the calculation. The first angle was obtained based on the depth of cut ap . The second angle was set to 5 deg. a priori. Finally, their median was also set to the third angle, and the average calculation was conducted with t_{uct} obtained using these angles.

DEMONSTRATIONS AND DISCUSSION

Demonstrations of the tool condition parameters will be provided in this section. The demonstrations were conducted under the three conditions with a variation of tool rotational speed and feed rate. They were also performed under the condition that a cutting area entirely exists in front of the cutting-related part of filleted end mill. Moreover, the influence of tool orientation on each parameter was investigated in filleted end milling. The discussion will also be made with visualizing characteristics of these parameters. Three machining conditions used in the demonstration are shown in Table 1. The condition 1 was set with reference to recommended conditions listed in several tool catalogs. The tool rotational speed s in condition 2 was twice as high as that in condition 1. The feed rate f in condition 3 was two times faster than that of condition 1. The tool diameter of end mill was set on the basis of a commonly-used size, and the tool had two straight cutting edges. The unit of angle was set as deg. to aid an intuitive understanding.

The influence of tool orientation on sl_{fd} is shown in Figure 5. The same results were obtained under the all conditions. These results means that sl_{fd} depended strictly on tool posture in filleted end milling.

Table 1. The machining conditions in filleted end milling

Specification	Condition 1	Condition 2	Condition 3
Tool radius, R [mm]	6.0	6.0	6.0
Tool tip, R_{cr} [mm]	4.0	4.0	4.0
The number of tooth, n_{ce}	2	2	2
Depth of cut, ap [mm]	0.2	0.2	0.2
Tool rotational speed, s [min^{-1}]	1400	2800	1400
Feed rate, f [mm/min]	260	260	520

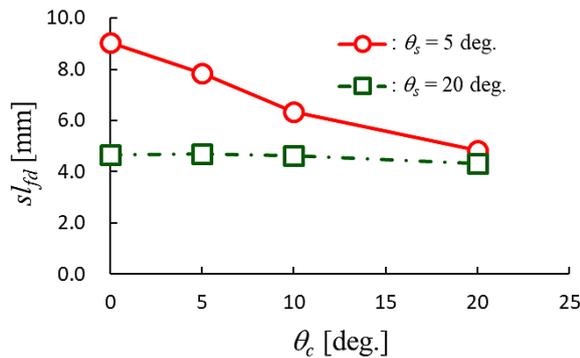


Fig. 5. Influence of θ_s and θ_c on sl_{fd} under the all conditions

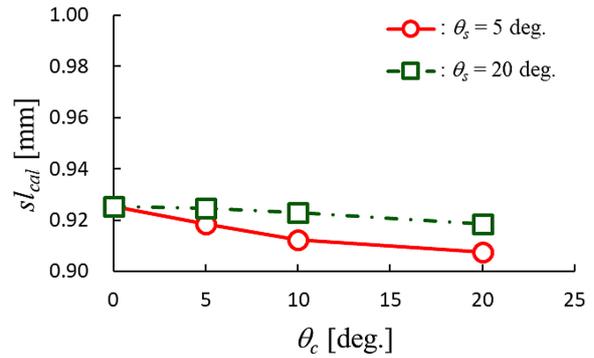


Fig. 7. Influence of θ_s and θ_c on sl_{cal} under the condition 2

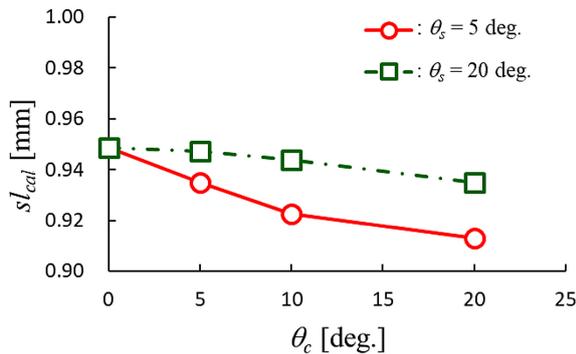


Fig. 6. Influence of θ_s and θ_c on sl_{cal} under the condition 1

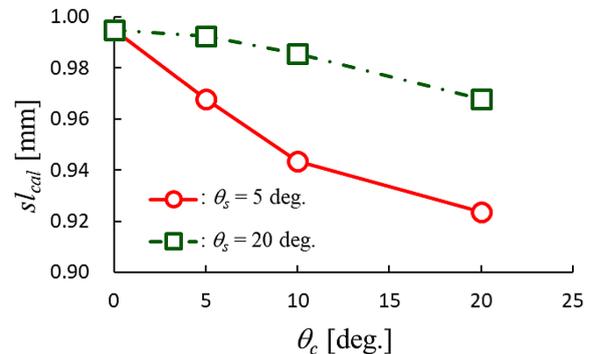


Fig. 8. Influence of θ_s and θ_c on sl_{calh} under the condition 3

In Figure 5, each curve for respective θ_s in graph legends represented decreasing tendency with increasing θ_c in any case and seemingly straight decline. Moreover, the differences between each curve became gradually smaller with increasing θ_c . The results denoted that the values of sl_{fd} appeared to converge towards a certain value with increasing θ_c . As an example of numerical results, when $\theta_c = 20$ deg., the values of sl_{fd} were 4.82 mm for θ_s with 5 deg. and 4.32 mm for θ_s with 20 deg. From the numerical results, the values of sl_{fd} are likely to become convergent in the case of θ_c with more than 20 deg.

The influence of tool orientation on sl_{cal} is given in Figures 6, 7 and 8. There were differences

between each condition since sl_{cal} depended essentially on a path interval along the feed direction of a tool. In these figures, each curve for respective θ_s in graph legends represented decreasing tendency with increasing θ_c in any case. The differences between each curve became larger with increasing θ_c , whereas it could be presumed that there existed the limit of sl_{cal} in the case of θ_c having an angle more than 20 deg. Although a certain line graph in condition 3 was seemingly observed as a precipitous decrease, the all results indicated that contact arc length was numerically unaltered in any case. In the pre-determined condition of z , the values of sl_{cal} were 0.95 mm in any case when $\theta_c = 0$ deg. in condition 1. The values were 0.93 mm in any case when $\theta_c = 0$

deg. in condition 2. They were 0.99 mm in any case when $\theta_c = 0$ deg. in condition 3. In addition, when $\theta_c = 20$ deg., the values of sl_{cal} were 0.91 mm for θ_s with 5 deg. and 0.93 mm for θ_s with 20 deg. in condition 1. The values were 0.91 mm for θ_s with 5 deg. and 0.92 mm for θ_s with 20 deg. in condition 2. They were 0.92 mm for θ_s with 5 deg. and 0.97 mm for θ_s with 20 deg. in condition 2. From the numerical values, there were noticeable differences under the case that θ_s and θ_c equal 20 deg.

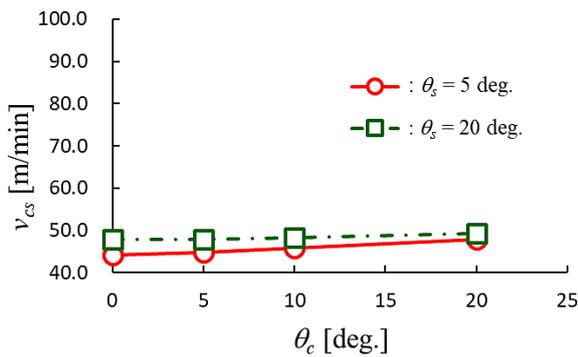


Fig. 9. Influence of θ_s and θ_c on v_{CS} under the conditions 1 and 3

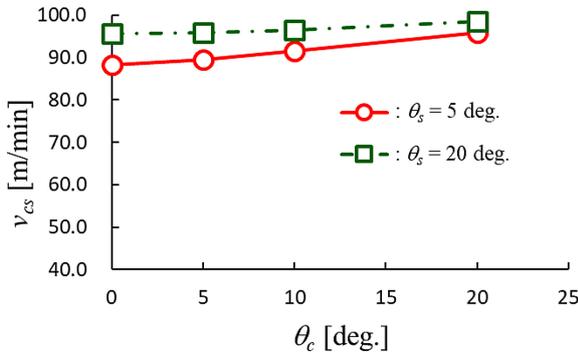


Fig. 10. Influence of θ_s and θ_c on v_{CS} under the condition 2

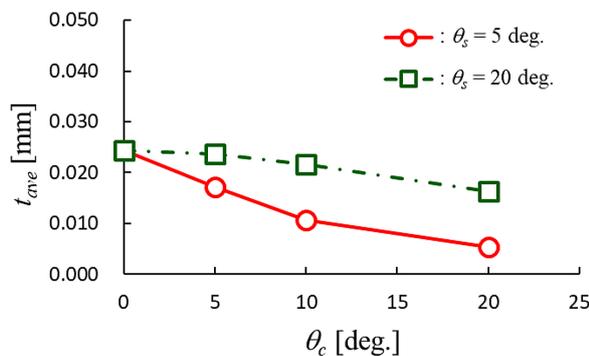


Fig. 11. Influence of θ_s and θ_c on t_{ave} under the condition 1

The influence of tool orientation on v_{CS} is represented in Figures 9 and 10. The same results were observed under the conditions 1 and 3, whereas the different result was obtained under the condition 2. In these figures, each curve for respective θ_s in graph legends showed slowly increasing tendency with increasing θ_c in any case. The increasing tendency considerably diminished with increasing θ_s . Moreover, the differences between each curve became smaller with increasing θ_c . In conditions 1 and 3, when $\theta_s = 20$ deg. and $\theta_c = 5$ deg., the value of v_{CS} was 47.92 m/min. Likewise, when $\theta_s = 5$ deg. and $\theta_c = 20$ deg., the value of v_{CS} was 47.92 m/min. In condition 2, when $\theta_s = 20$ deg. and $\theta_c = 5$ deg., the value of v_{CS} was 95.84 m/min. Similarly, when $\theta_s = 5$ deg. and $\theta_c = 20$ deg., the value of v_{CS} was 95.84 m/min. In the four machining states, the value of θ was 20.52 deg. It was obvious from the results that the value of v_{CS} was completely identical under the same θ and depended strongly on s .

The influence of tool orientation on t_{ave} is displayed in Figures 11, 12, and 13. There were differences between each condition since t_{ave} depended

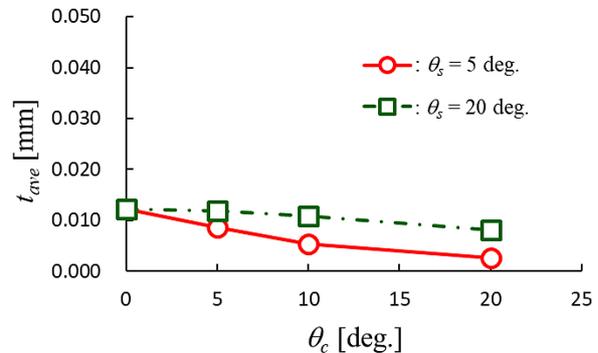


Fig. 12. Influence of θ_s and θ_c on t_{ave} under the condition 2

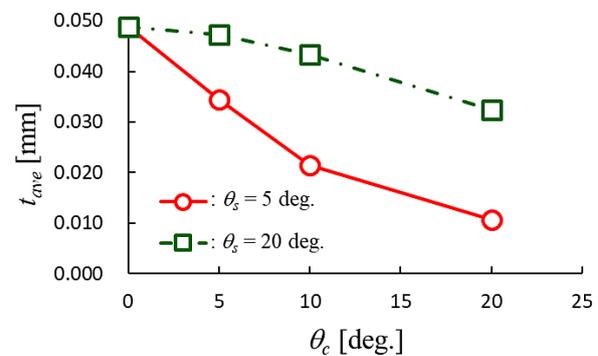


Fig. 13. Influence of θ_s and θ_c on t_{ave} under the condition 3

essentially on a path interval along the feed direction of a tool. The feature was very similar to that of sl_{cal} . In these figures, each curve for respective θ_s in graph legends indicated decreasing tendency with increasing θ_c in any case. The differences between each curve became larger with increasing θ_c , whereas it can be presumed that there existed the limit of t_{ave} in the case of θ_c having an angle more than 20 deg. The results implied that an instantaneous cutting force acting on a cutting edge decreased with increasing θ . With reference to the variation of t_{ave} , the decreasing rate would be especially prominent in the small value of θ_s .

CONCLUSION

This study dealt with theoretical investigations regarding tool condition parameters. The computational analyses were demonstrated to determine machining conditions after the geometrical modeling was provided to express multi-axis filleted end milling. The demonstrations with three machining conditions were made to compare the results under the conditions with some variations of θ_s , θ_c , s , and f . As a result, some characteristics of tool condition parameters were revealed from the visual evidences and discussion. One of the characteristics was that sl_{fd} depended strictly on tool posture in filleted end milling. Moreover, sl_{cal} depended essentially on a path interval along the feed direction of a tool. The results obtained from the demonstrations also represented that t_{ave} could be indirectly predictable from sl_{cal} .

As a future work, the further detailed analysis will be conducted in a wide variety of conditions, and the experimental verification will be made to evaluate validity and applicability of tool condition parameters proposed in this study.

Acknowledgments

The authors would like to thank the financial support provided by OSG Fund and the research grant from Faculty of Science and Technology, Seikei University.

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